**Name: \_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_**

**Instructor: \_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_**

**Term: \_\_\_\_\_\_\_\_\_\_\_\_\_\_**

* General Guidelines and Grading
  + Throughout the semester there will key concepts that will be included in this notebook. A table of contents with page numbers will be kept and updated in class. The notebook will be scored on a 100 point basis.
  + Notebooks will be graded COMPETITIVELY(see note below) based on the following

1. Quality
2. Accuracy
3. Organization
4. Neatness
5. Completeness

Note: Competitively implies those notebooks following the five criteria above “best” will receive the highest scores.

* + The notebook will be checked at various points during the semester. Points will be awarded each time the notebook is checked. These dates will be announced in class.
  + You will have a chance to correct and alter your notebook and resubmit it for a final time. It will be graded one last time based on correctness, neatness, and usability for future classes.
    - This notebook should be your BEST work. As a general guideline anyone in a Trigonometry course (or beyond) should to be able to read and understand your material.
    - The notebook will at this point be graded on a competitive scale.
    - If you choose to redo any pages of the notebook (recommended) please include the graded page in front of EACH corrected page so that I can view your old work and your revised work on a page by page basis. Otherwise just include the non-corrected page.
    - Only exceptionally correct, useable, and visually impressive notebooks will receive full credit.

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| B | [Define tangent, cotangent, secant, cosecant using sine, cosine](#define_tangent) | 3 |  |  |  |
| C | [Trigonometric Table](#trig_table) | 4 |  |  |  |
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| N | [Prove Difference Identity for Cosine. Include sketch](#Prove_diff_id_cos). | 11 |  |  |  |
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**[Define sine and cosine](#TOC)**. Label triangle below using , x, y and r. Be sure to indicate if it is a right triangle.

**[Define tangent, cotangent, secant, cosecant using sine, cosine](#TOC)**, as well as by using the terms “opposite”, “adjacent”, “hypotenuse”, and thirdly, as well as in terms of and as referenced above.

**[Trigonometric Table](#TOC)**

Complete the Trigonometric Table.

|  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| Deg | Ref | Quadrant | Radians | cos θ | sin θ | tan θ | sec θ | csc θ | cot θ |
| -90 |  |  |  |  |  |  |  |  |  |
| -60 |  |  |  |  |  |  |  |  |  |
| -45 |  |  |  |  |  |  |  |  |  |
| -30 |  |  |  |  |  |  |  |  |  |
| 0 | 0 |  | 0 | 0 | 1 |  |  |  | 0 |
| 30 | 30 |  |  |  |  |  |  |  |  |
| 45 | 45 |  |  |  |  |  |  |  |  |
| 60 | 60 |  |  |  |  |  |  |  |  |
| 90 | 90 |  |  |  |  |  |  |  |  |
| 120 | 60 |  |  |  |  |  |  |  |  |
| 135 | 45 |  |  |  |  |  |  |  |  |
| 150 | 30 |  |  |  |  |  |  |  |  |
| 180 | 0 |  |  |  |  |  |  |  |  |
| 210 | 30 |  |  |  |  |  |  |  |  |
| 225 | 45 |  |  |  |  |  |  |  |  |
| 240 | 60 |  |  |  |  |  |  |  |  |
| 270 | 90 |  |  |  |  |  |  |  |  |
| 300 | 60 |  |  |  |  |  |  |  |  |
| 315 | 45 |  |  |  |  |  |  |  |  |
| 330 | 30 |  |  |  |  |  |  |  |  |
| 360 | 0 |  |  |  |  |  |  |  |  |

# Signs of Functions

# Fill in the [**sign for each trig function’s value**](#TOC)**:**

|  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- |
| Quadrant | X axis (adj side) | Y axis (opp side) |  |  |  |  |  |  |
| 1 | + | + |  |  |  |  |  |  |
| 2 | - | + |  |  |  |  |  |  |
| 3 | - | - |  |  |  |  |  |  |
| 4 | + | - |  |  |  |  |  |  |

# **[Domains and ranges of functions](#TOC)**

Fill in each blank

|  |  |  |
| --- | --- | --- |
| Function | Domain | Range |
|  |  |  |
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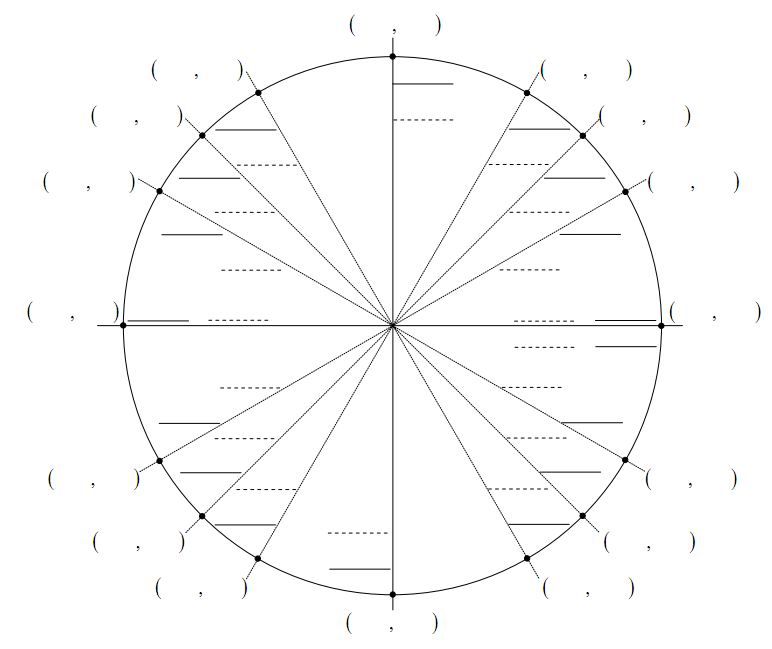
## **[Inverse Trig Function Restrictions](#TOC)**

Fill in restrictions ***on the domain of each*** of the listed ***functions*** so that the inverse of each will itself be a function. Then fill in the corresponding range for each.

|  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- |
|  |  |  |  |  |  |  |
| Domain |  |  |  |  |  |  |
| Range |  |  |  |  |  |  |

## **[Unit Circle](#TOC).**

For each ‘key’ point on the unit circle, include the degrees, radians, and coordinates of the associated points.



**[Graph and on same graph over interval [-2π, 2π].](#TOC)** Choose appropriate scale and label. Give the domain and range of each function. Show asymptotes for the graph.



**[Graph y = cos x and y = sec x on same graph over interval [-2π, 2π]](#TOC)**. Choose appropriate scale and label. Give the domain and range of each function. Show asymptotes for the y = sec x graph.



**[Graph y = tan x over at least 2 periods](#TOC)**. Choose appropriate scale and label. Give the domain and range. Show asymptotes.



**[Graph y = cot x over at least 2 periods](#TOC)**. Choose appropriate scale and label. Give the domain and range. Show asymptotes.



**[Graph y = cos(4x) and](#TOC)**  on same set of axes over at least one period for each function.

## graph_paper_1up**[Graph over at least one period](#TOC). Give domain and range.**



****[**Graph  and on same set of axes over at least one period**](#TOC)**.** Show asymptotes for the cosecant graph.

**[Prove the difference identity for cosine](#TOC).**

Prove: . Include all necessary figures in your sketch below.

## **[Prove the remaining sum and difference identities for sine, cosine, and tangent](#TOC).**

1. 
2. 
3. 
4. 
5. 

**[Write in each identity](#TOC)**.

|  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- |
| Pythagorean Identities | | Quotient Identities | | Reciprocal Identities | | |
|  | | Tan θ = Sin θ/ Cos θ | |  | |  |
|  | | Cot θ = Cos θ/ Sin θ | |  | |  |
|  | |  | |  | |  |
| Reflective Identities | | | Negative Angle Identities | | | |
|  |  | |  | |  | |
|  |  | |  | |  | |
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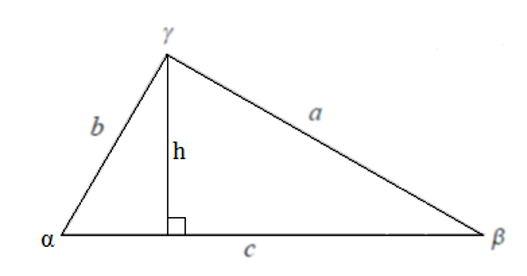
|  |  |  |  |
| --- | --- | --- | --- |
| Co-function Identities | | | Angle Sum/ Difference Identities |
|  |  | |  |
|  |  | |  |
|  |  | |  |
| Double Angle Identities | | Power Reducing Identities | Half Angle Identities |
|  | |  |  |
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[**Prove these Fundamental Identities**](#TOC).



Negative angle identities (show sketch to right)

**[Derive/Prove the laws of sines and cosines](#TOC)**. (Include the related diagram.)

 Prove only one law of cosines but list all three.)

## **[Graph y = tan](#TOC)[-1](#TOC)[(x)](#TOC):**

Give the domain and range of y = tan-1(x). Hint: Refer to y = tan x.

Domain: \_\_\_\_\_\_\_\_\_\_\_\_\_\_ Range: \_\_\_\_\_\_\_\_\_\_\_\_\_\_

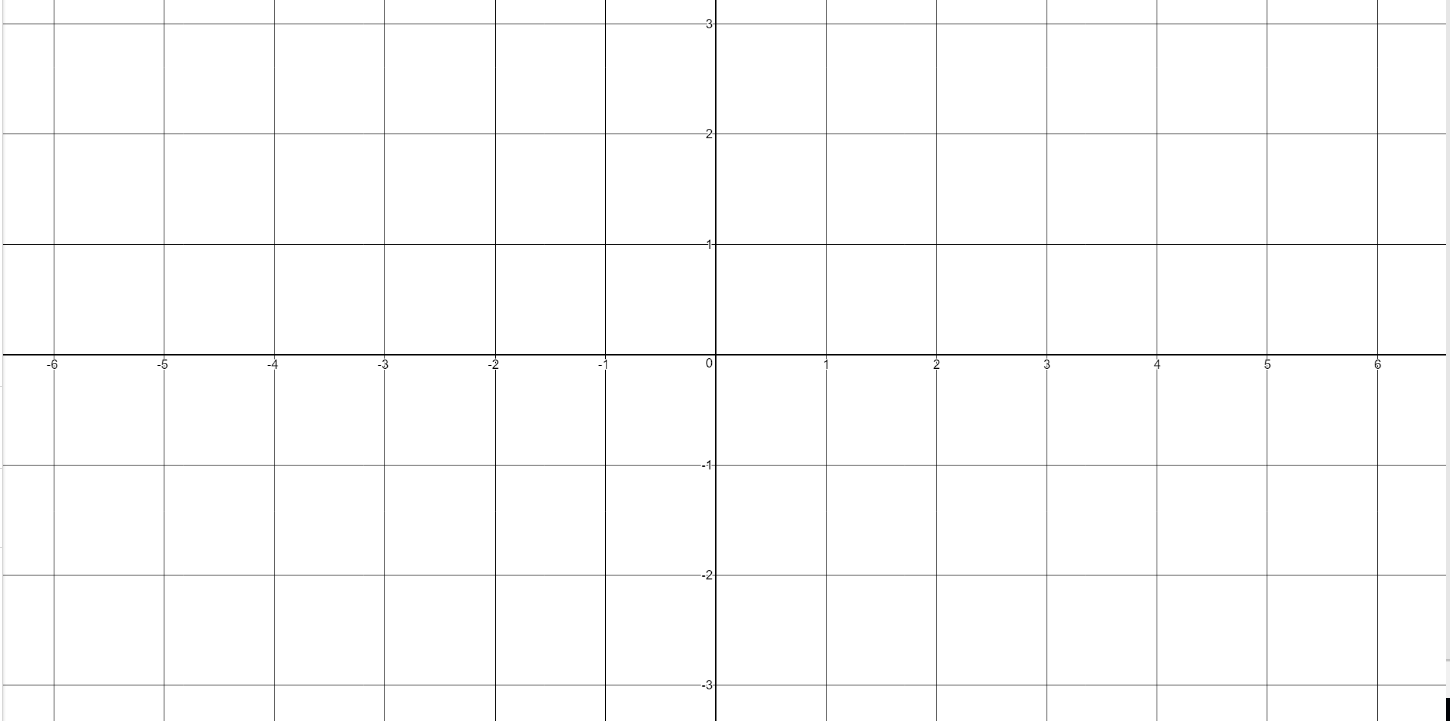
Graph as follows. Label “y” axis in radians.

1. Fill out table 1 below
2. Fill out table 2 below by filling in the corresponding points for
3. Plot the corresponding points and graph show asymptote(s) & label the points.

Table 1. Table 2.

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## **[Graph y = sec](#TOC)[-1](#TOC)[(x)](#TOC):**

Give the domain and range of y = sec-1(x). Hint: Refer to y = sec x.

Domain: \_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_ Range: \_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_

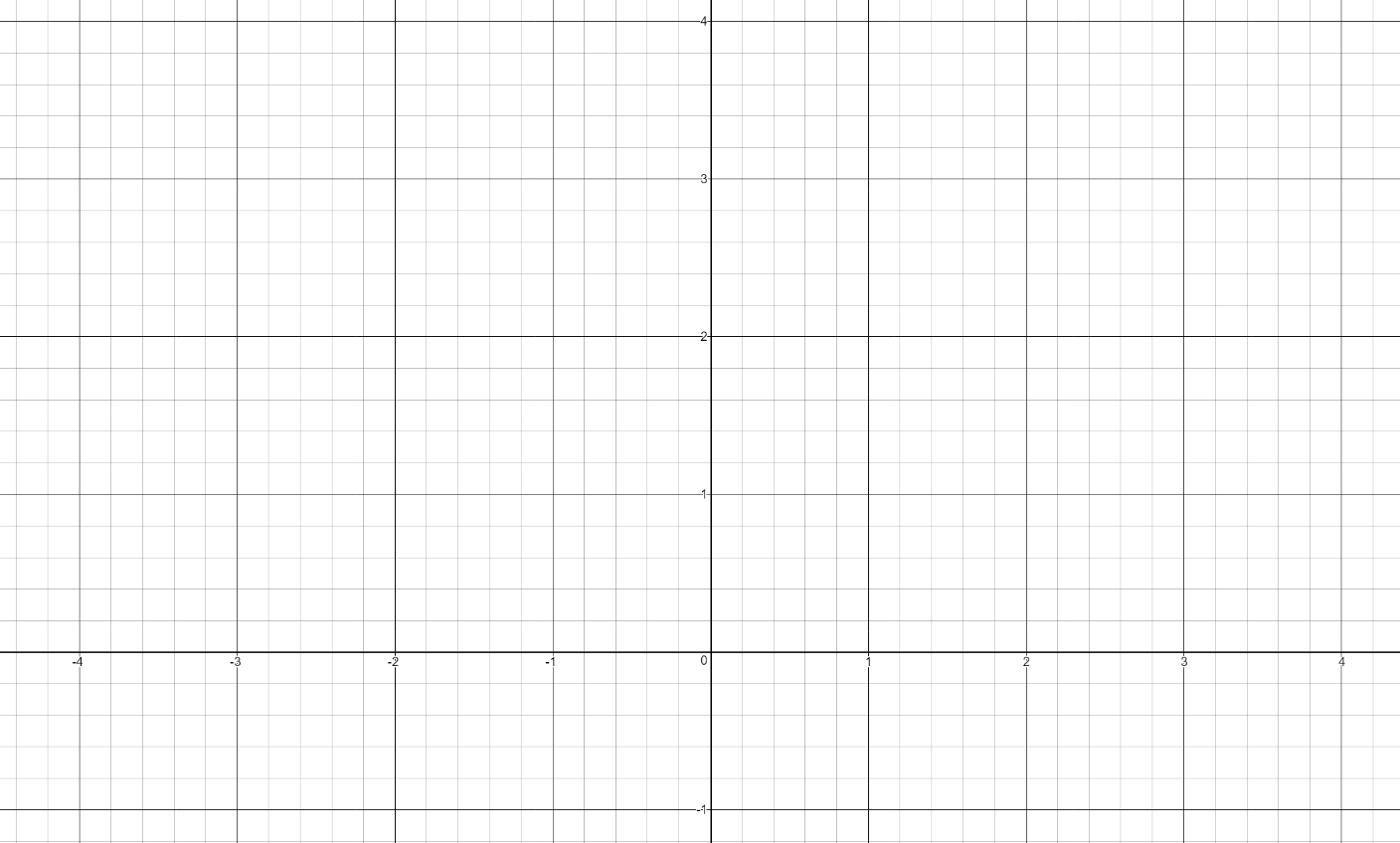
Graph (arcsec(x)) as follows. Label “y” axis in radians.

1. Fill out table 1 below
2. Fill out table 2 below by filling in the corresponding points for
3. Plot the corresponding points and graph how asymptote(s) & label the points.

Table 1. Table 2.

|  |  |
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**[Graph the remaining 4 inverse trig functions](#TOC)**. Show any asymptotes. Scale axes. Label points. Give domain and range of each.



|  |  |  |  |  |
| --- | --- | --- | --- | --- |
|  | |  |  | |
| Domain: | Range: | Domain: | Range: |
|  | |  | |
| Domain: | Range: | Domain | Range: |

